Maximum Marks: 80

CLASS X (2019-20) MATHEMATICS STANDARD(041) SAMPLE PAPER-9

Time: 3 Hours

General Instructions :

- (i) All questions are compulsory.
- (ii) The questions paper consists of 40 questions divided into 4 sections A, B, C and D.
- (iii) Section A comprises of 20 questions of 1 mark each. Section B comprises of 6 questions of 2 marks each. Section C comprises of 8 questions of 3 marks each. Section D comprises of 6 questions of 4 marks each.
- (iv) There is no overall choice. However, an internal choices have been provided in two questions of 1 mark each, two questions of 2 marks each, three questions of 3 marks each, and three questions of 4 marks each. You have to attempt only one of the alternatives in all such questions.
- (v) Use of calculators is not permitted.

Section A

Q.1-Q.10 are multiple choice questions. Select the most appropriate answer from the given options.

- Which of the following rational number have non-1. terminating repeating decimal expansion? [1]
 - (a) $\frac{31}{3125}$ (b) $\frac{71}{512}$
 - (c) $\frac{23}{200}$ (d) None of these

Ans : (d) None of these

 $3125,\ 512$ and 200 has factorization of the form $2^m \times 5^n$ (where *m* and *n* are whole numbers). So given fractions has terminating decimal expansion.

If the sum of the zeroes of the polynomial 2. $f(x) = 2x^3 - 3kx^2 + 4x - 5$ is 6, then the value of k is [1] (b) -2(a) 2 (c) 4 (d) - 4

Ans: (c) 4

Sum of the zeroes $=\frac{3k}{2}$ $6 = \frac{3k}{2}$ $k = \frac{12}{3} = 4$

- A fraction becomes 4 when 1 is added to both the 3. numerator and denominator and it becomes 7 when 1 is subtracted from both the numerator and denominator. The numerator of the given fraction is [1](b) 3
 - (a) 2
 - (c) 5 (d) 15

Ans: (d) 15

Let the fraction be $\frac{x}{y}$,

$$\frac{x+1}{y+1} = 4 \qquad ...(1)$$

and

- Solving (1) and (2),
- x = 15, y = 3,We have x = 15i.e.

 $\frac{x-1}{u-1} = 7$

4. $(x^2 + 1)^2 - x^2 = 0$ has (a) four real roots [1] (b) two real roots (c) no real roots (d) one real root **Ans** : (c) no real roots Given equation is, $(x^{2}+1)^{2}-x^{2}=0$ $x^{4} + 1 + 2x^{2} - x^{2} = 0$ [:: $(a + b)^{2} = a^{2} + b^{2} + 2ab$]

$$x^{4} + x^{2} + 1 = 0$$
$$x^{2} = y$$
$$(x^{2})^{2} + x^{2} + 1 = 0$$

 $y^2 + y + 1 = 0$ On comparing with $ay^2 + by + c = 0$, a = 1, b = 1 and c = 1we get $D = b^2 - 4ac$ Discriminant, $=(1)^{2}-4(1)(1)$ = 1 - 4 = -3

Since, D < 0

Let.

i.e.,
$$y^2 + y + 1 = 0$$

 $x^4 + x^2 + 1 = 0$

 $(x^2+1)^2 - x^2 = 0$ has no real roots. or

An AP starts with a positive fraction and every 5. alternate term is an integer. If the sum of the first 11 terms is 33, then the fourth term is [1] (a) 2 (b) 3

(c)
$$5$$
 (d) 6

ie

Given,

$$\frac{11}{2}[2a+10d] = 33 \Rightarrow a+5d = 3$$

 $S_{11} = 33$

$$a_6 = 3 \Rightarrow a_4 =$$

[Since, Alternate terms are integers and the given sum is possible]

2

6. C is the mid-point of PQ, if P is (4, x), C is (y, -1)and Q is (-2, 4), then x and y respectively are [1] (a) -6 and 1 (b) -6 and 2 (c) 6 and -1(d) 6 and -2

Ans : (a) -6 and 1

Since, C(y, -1) is the mid-point of P(4, x) and Q(-2,4).

...(2)

7. In the adjoining figure, the length of BC is [1]



In $\triangle ABC$,

$$\sin 30^{\circ} = \frac{BC}{AC}$$
$$\frac{1}{2} = \frac{BC}{6}$$
$$BC = 3 \text{ cm}$$

- 8. The volume of a largest sphere that can be cut from cylindrical log of wood of base radius 1 m and height 4 m, is [1]
 - (a) $\frac{16}{3} \pi \text{ m}^3$ (b) $\frac{8}{3} \pi \text{ m}^3$ (c) $\frac{4}{3} \pi \text{ m}^3$ (d) $\frac{10}{3} \pi \text{ m}^3$ **Ans**: (c) $\frac{4}{3} \pi \text{ m}^3$ Volume of sphere $= \frac{4}{3} \pi r^3 = \frac{4}{3} \pi (1)^3$ $= \frac{4}{3} \pi m^3$
- **9.** If the coordinates of the point of intersection of less than ogive and more than ogive is (13.5,20), then the value of median is [1]
 - (a) 13.5 (b) 20
 - (c) 33.5 (d) 7.5

Ans : (a) 13.5

The abscissa of point of intersection gives the median of the data. So, median is 13.5.

10. A three digit number is to be formed using the digits 3, 4, 7, 8 and 2 without repetition. The probability that it is an odd number is [1]

(a)
$$\frac{2}{5}$$
 (b) $\frac{1}{5}$
(c) $\frac{4}{5}$ (d) $\frac{3}{5}$
Ans: (a) $\frac{2}{5}$

(Q.11-Q.15) Fill in the blanks.

11. theorem states that if a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, the other two sides are divided in the same ratio. [1]

Ans : Basic proportionality

12. Point on the X-axis which is equidistant from (2, -5) and (-2,9) is [1]
Ans: (-7,0)

 \mathbf{or}

Relation between x and y if the points (x, y), (1, 2)and (7, 0) are collinear is [1] Ans : x + 3y = 7

- 13. Triangle in which we study trigonometric ratios is called [1]Ans : Right Triangle
- 14. The common point of a tangent to a circle and the circle is called [1]Ans : Point of contact
- 15. Only two can be drawn to a circle from an external point. [1]Ans : Tangents

(Q.16-Q.20) Answer the following

16. A ladder, leaning against a wall, makes an angle of 60° with the horizontal. If the foot of the ladder is 2.5 m away from the wall, find the length of the ladder. [1] Ans:

Let the length of ladder be x. As per given in question we have drawn figure below.



17. The diameter of two circle with centre A and B are 16 cm and 30 cm respectively. If area of another circle with centre C is equal to the sum of areas of these two circles, then find the circumference of the circle with centre C. [1]

Ans :

As we know that, Area of circle $= \pi r^2$, Let the radius of circle with centre C = RAccording to question we have,

$$\pi (8)^{2} + \pi (15)^{2} = \pi R^{2}$$

$$64\pi + 225\pi = \pi R^{2}$$

$$289\pi = \pi R^{2}$$

$$R^{2} = 289 \text{ or } R = 17 \text{ cm}$$

Circumference of circle

18. 12 solid spheres of the same size are made by melting a solid metallic cone of base radius 1 cm and height of 48 cm. Find the radius of each sphere. [1]
Ans :

No. of spheres	= 12
Radius of cone,	r = 1 cm
Height of the cone	= 48

Volume of 12 spheres = Volume of cone

Let the radius of sphere be R.

$$12 \times \frac{4}{3}\pi R^3 = \frac{1}{3}\pi r^2 h$$
$$12 \times \frac{4}{3}\pi R^3 = \frac{1}{3}\pi \times (1)^2 \times 48$$
$$R^3 = 1$$
$$R = 1 \text{ cm}$$
or

Three cubes of iron whose edges are 3 cm, 4 cm and 5 cm respectively are melted and formed into a single cube, what will be the edge of the new cube formed ? Ans :

Let the edge of single cube be x cm.

Volume of single cube= Volume of three cubes

$$x^{3} = (3)^{3} + (4)^{3} + (5)^{3}$$

= 27 + 64 + 125 = 216
$$x = 6 \text{ cm}$$

In the following frequency distribution, find the median class.
 [1]

Height (in	104-	145-	150-	155-	160-	165-	-
cm)	145	150	155	160	165	170	
Frequency	5	15	25	30	15	10	

Ans :

Height	Frequency	c.f.
140-145	5	5
145-150	15	20
150-155	25	45
155-160	30	75
160-165	15	90
165-170	10	100
	$\sum f = 100$	

$$N = 100$$

$$\Rightarrow \qquad \frac{N}{2} \text{ th term } = \frac{100}{2} = 50 \text{ th Mean}$$

Hence, Median class in 155-160.

20. A letter of English alphabet is chosen at random. Determine the probability that the chosen letter is a

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Ans :

In the English language there are 26 alphabets. Consonant are 21. The probability of chosen a consonant

$$P = \frac{21}{26}$$

Section **B**

21. Using Euclid's algorithm, find the HCF of 240 and 228.[2]

Ans :

We have $240 = 228 \times 1 + 12$ and $228 = 12 \times 19 + 0$ Hence, HCF of 240 and 228 = 12

22. Solve for x: $x^2 - (\sqrt{3} + 1)x + \sqrt{3} = 0$ [2] Ans:

w.f.
$$x^2 - (\sqrt{3} + 1)x + \sqrt{3} = 0$$

 $x^2 - \sqrt{3}x - 1x + \sqrt{3} = 0$
 $x(x - \sqrt{3}) - 1(x - \sqrt{3}) = 0$
 $(x - \sqrt{3})(x - 1) = 0$
Thus $x = \sqrt{3}, x = 1$

23. In the given figure, G is the mid-point of the side PQ of ΔPQR and GH||QR. Prove that H is the midpoint of the side PR or the triangle PQR. [2]



Ans :

Since G is the mid-point of PQ we have

$$PG = GQ$$
$$\frac{PG}{GQ} = 1$$

According to the question, GH||QR, thus

$$\frac{PG}{GQ} = \frac{PH}{HR}$$
(By BPT)
$$1 = \frac{PH}{HR}$$

PH = HR.

Hence proved.

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Hence, H is the mid-point of PR.

 \mathbf{or}

In a rectangle ABCD, E is a point on AB such that $AE = \frac{2}{3}AB$. If AB = 6 km and AD = 3 km, then find DE. Ans:

As per given condition we have drawn the figure

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We have

 $AE = \frac{2}{3}AB = \frac{2}{3} \times 6 = 4 \text{ km}$ In right triangle ADE,

> $DE^2 = (3)^2 + (4)^2 = 25$ DE = 5 km

Thus

- 24. A box contains 8 black beads and 12 white beads. Another box contains 9 black beads and 6 white beads. One bead from each box is taken. [2]
 - (a) What is the probability that both beads are black?
 - (b) What is the probability of getting one black bead and one white bead ?

Ans :

Total number of cases, $20 \times 15 = 300$ Both are black $8 \times 9 = 72$

- (a) Probability of getting both black $=\frac{72}{300}=\frac{6}{25}$
- One black and one white $8 \times 6 + 12 \times 9 = 156$ (b) Probability $=\frac{156}{300}=\frac{13}{25}$
- 25. The mean and median of 100 observation are 50 and 52 respectively. The value of the largest observation is 100. It was later found that it is 110. Find the true mean and median. [2]

Ans:

 \Rightarrow

 $50 = \frac{\sum fx}{100}$

 \Rightarrow

$$\sum fx' = 5000 - 100 + 110 = 5010$$

:. Correct Mean
$$=\frac{5010}{100} = 50.1$$

Median will remain same *i.e.* median = 52.

Mean $= \frac{\sum fx}{\sum f}$

 $\sum fx = 5000$

or

Find the sum of the lower limit of the median class and the upper limit of the modal class :

Classes	10- 20	20- 30	30- 40	40- 50	50- 60	60- 70
Frequency	1	3	5	9	7	3
Ans:						

Class	10- 20	20- 30	30- 40	40- 50	50- 60	60- 70
Frequency	1	3	5	9	7	3
Cumulative Frequency	1	4	9	18	25	28

Median
$$= \frac{N}{2}$$
th
 $= \frac{28}{2} = 14$ th term

 \therefore Median class : 40-50 \Rightarrow Lower limit = 40

and Modal class : $40-50 \Rightarrow$ Upper limit = 50

Their sum = 40 + 50 = 90

26. Due to sudden floods, some welfare associations jointly requested the government to get 100 tents fixed immediately and offered to contribute 50% of the cost. If the lower part of each tent is of the form of a cylinder of diameter 4.2 m and height 4 m with the conical upper part of same diameter but of height 2.8 m and the canvas to be used cost ₹100 per sq.m, find the amount, the associations will have to pay. [Use $\pi = \frac{22}{7}$] [2]

Ans :

ar

A

Given, Height of upper conical part

$$h = 2.8 \text{ m}$$

and radius, $r = \frac{4.2}{2} = 2.1 \text{ m}$
Slant height, $l = \sqrt{h^2 + r^2}$
 $= \sqrt{(2.8)^2 + (2.1)^2}$
 $= \sqrt{7.84 + 4.41} = 3.5 \text{ m}$
Surface area of tent $= 2\pi rh + \pi rl$
Area of canvas for 1 tent
 $= 2 \times \frac{22}{\pi} \times 2.1 \times 4 + \frac{22}{\pi} \times 2.1 \times 3.5$

$$= 6.6(8 + 3.5)$$

 $= 6.6 \times 11.5 \,\mathrm{m}^2$

Area for 100 tents $= 6.6 \times 11.5 \times 100$

$$= 66 \times 115 \,\mathrm{m^2} = 7590 \,\mathrm{m^2}$$

Cost of 100 tents = ₹ 7590 × 100

$$50 \% \text{ cost} = \frac{50}{100} \times 7590 \times 100$$

=₹379500

Value : Helping the flood victims.

Section C

27. Find the HCF, by Euclid's division algorithm of the numbers 92690, 7378 and 7161. [3]Ans :

By using Euclid's Division Lemma, we have

$$92690 = 7378 \times 12 + 4154$$

$$7378 = 4154 \times 1 + 3224$$

$$4154 = 3224 \times 1 + 930$$

$$3224 = 930 \times 3 + 434$$

$$930 = 434 \times 2 + 62$$

$$434 = 62 \times 7 + 0$$

HCF (92690, 7378) = 62

Now, using Euclid's Division Lemma on 7161 and 62, we have

$$7161 = 62 \times 115 + 31$$

 $62 = 31 \times 2 + 0$ Thus HCF (7161, 62) = 31Hence, HCF of 92690, 7378 and 7161 is 31.

or

Find HCF and LCM of 16 and 36 by prime factorization and check your answer.

Ans :

Finding prime factor of given number, we have,

$$\begin{split} 16 &= 2 \times 2 \times 2 \times 2 = 2^4 \\ 36 &= 2 \times 2 \times 3 \times 3 = 2^2 \times 3^2 \\ &\text{HCF}(16, \ 36) = 2 \times 2 = 4 \\ &\text{LCM} \ (16, \ 36) = 2^4 \times 3^2 \\ &= 16 \times 9 = 144 \end{split}$$
 To check HCF and LCM by using formula
$$&\text{HCF}(a, b) \times \text{LCM}(a, b) = a \times b \end{split}$$

LHS = RHS

or,
$$4 \times 144 = 16 \times 36$$

 $576 = 576$

Thus

28. Solve for x:

HC

$$\frac{1}{(x-1)(x-2)} + \frac{1}{(x-2)(x-3)} = \frac{2}{3}; x \neq 1, 2, 3$$
Ans:

We have
$$\frac{1}{(x-1)(x-2)} + \frac{1}{(x-2)(x-3)} = \frac{2}{3}$$
$$\frac{x-3+x-1}{(x-1)(x-2)(x-3)} = \frac{2}{3}$$
$$\frac{2x-4}{(x-1)(x-2)(x-3)} = \frac{2}{3}$$
$$\frac{2(x-2)}{(x-1)(x-2)(x-3)} = \frac{2}{3}$$
$$\frac{2}{(x-1)(x-3)} = \frac{2}{3}$$
$$3 = (x-1)(x-3)$$
$$x^2 - 4x + 3 = 3$$
$$x^2 - 4x = 0$$
$$x(x-4) = 0$$

Thus x = 0 or x = 4

29. The sum of *n* terms of an A.P. is $3n^2 + 5n$. Find the A.P. Hence find its 15^{th} term. [3]Ans :

Let the first term be a, common difference be d, nth term be a_n and sum of n term be S_n

Now

$$S_{n} = 3n^{2} + 5m$$

$$S_{n-1} = 3(n-1)^{2} + 5(n-1)$$

$$= 3(n^{2} + 1 - 2n) + 5n - 5$$

$$= 3n^{2} + 3 - 6n + 5n - 5$$

$$= 3n^{2} - n - 2$$

$$a_{n} = S_{n} - S_{n-1}$$

$$= 3n^{2} + 5n - (3n^{2} - n - 2)$$

$$= 6n + 2$$

Thus A.P. is 8, 14, 20,

or

Divide 56 in four parts in A.P. such that the ratio of the product of their extremes $(1^{st} \text{ and } 4^{rd})$ to the product of means $(2^{nd} \text{ and } 3^{rd})$ is 5:6.

 $a_{15} = a + 14d = 8 + 14(6) = 92$

Ans :

Let the four numbers be a - 3d, a - d, a + d, a + 3dNow a - 3d + a - d + a + d + a + 3d = 56

$$4a = 56 \Rightarrow a = 14$$

Hence numbers are 14 - 3d, 14 - d, 14 + d, 14 + 3dNow, according to question.

$$(14 - 3d)(14 + 3d)$$

$$\frac{(14-3d)(14+3d)}{(14-d)(14+d)} = \frac{5}{6}$$

$$\frac{196-9d^2}{196-d^2} = \frac{5}{6}$$

$$6(196-9d^2) = 5(196-d^2)$$

$$6 \times 196 - 54d^2 = 5 \times 196 - 5d^2$$

$$(6-5) \times 196 = 49d^2$$

$$d^2 = \frac{196}{49} = 4$$

$$d = \pm 2$$
Thus numbers are
$$a - 3d = 14 - 3 \times 2 = 8$$

$$a - d = 14 - 2 = 12$$

$$a + d = 14 + 2 = 16$$

$$a + 3d = 14 + 3 \times 2 = 20$$

Thus required A.P is 8,12,16,20.

30. Two tangents TP and TQ are drawn to a circle with centre O from an external point T. Prove that [3] $\angle PTO = \angle OPQ$

Ans :

Now

[3]

As per question we draw figure shown below.



Let $\angle TPQ$ be θ . the tangent is perpendicular to the end point of radius,

$$\angle TPO = 90^{\circ}$$

 $\angle TPQ = \angle TPO - \theta$

 $= (90^{\circ} - \theta)$

Since, TP = TQ and opposite angels of equal sides are always equal, we have

$$\angle TQP = (90^{\circ} - \theta)$$

Now in
$$\Delta TPQ$$
 we have
 $\angle TPQ + \angle TQP + \angle PTQ = 180^{\circ}$

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$$90^{\circ} - \theta + 90^{\circ} - \theta + \angle PTQ = 180^{\circ}$$
$$\angle PTQ = 180^{\circ} - 180^{\circ} + 2\theta = 2\theta$$
Hence $\angle PTQ = 2\angle OPQ$.

- 31. Three Students Priyanka, Sania and David are Protesting against killing innocent animals for commercial purposes in a circular park of radius 20 m. They are standing at equal distance on its boundary by holding banners in their hands. [3]
 - (i) Find the distance between each of them? (ii) Which mathematical concept is used in it?

Ans :

(i) Let us assume that A, B and C are the position of Priyanka, Sania and David respectively on the boundary of circular park with centre O.

Draw $AD \perp BC$

Since the centre of the circle coincides with the centroid of the equilateral ΔABC .



$$20 = \frac{3}{2}AD$$
$$AD = 20 \times \frac{3}{2}$$
$$AD = 30 \text{ m}$$
Now, $AD \perp BC$, and let $AB = BC = CA = x$
$$BD = CD = \frac{1}{2}BC = \frac{x}{2}$$



In rt. ΔBDA , $\angle D = 90^{\circ}$ By Pythagoras Theorem, we have

4 D²

$$AB^{2} = BD^{2} + AD^{2}$$
$$x^{2} = \left(\frac{x}{2}\right)^{2} + (30)^{2}$$
$$x^{2} - \frac{x^{2}}{4} = 900$$
$$\frac{3}{4}x^{2} = 900$$
$$x^{2} = 900 \times \frac{4}{3} = 1200$$

 $x = \sqrt{1200} = 20\sqrt{3}$ Hence, distance between each of them is $20\sqrt{3}$. (ii) Properties of circle, equilateral triangle and Pythagorean theorem.

32. A 7 m long flagstaff is fixed on the top of a tower standing on the horizontal plane. From point on the ground, the angles of elevation of the top and bottom of the flagstaff are 60° and 45° respectively. Find the height of the tower correct to one place of decimal.

(Use $\sqrt{3} = 1.73$) [3]Ans :

As per given in question we have drawn figure below.



An aeroplane, when flying at a height of 4000 m from the ground passes vertically above another aeroplane at an instant when the angles of elevation of the two planes from the same point on the ground are 60° and 45° respectively. Find the vertical distance between the aeroplanes at that instant. (Use $\sqrt{3} = 1.73$)

Ans :

Let the height first plane be AB = 4000 m and the height of second plane be BC = x m. As per given in question we have drawn figure below.



Here $\angle BDC = 45^{\circ}$ and $\angle ADB = 60^{\circ}$ $\frac{x}{y} = \tan 45^{\circ} = 1 \Rightarrow x = y$ In ΔCBD , and in ΔABD , $\frac{4000}{y} = \tan 60^{\circ} = \sqrt{3}$ $y = \frac{4000\sqrt{3}}{3} = 2309.40 \text{ m}$ Thus vertical distance between two,

$$4000 - y = 4000 - 2309.40 = 1690.59 \text{ m}$$

33. A solid sphere of diameter 6 cm is dropped in a right circular cylindrical vessel partly filled with water. The diameter of the cylindrical vessel is 12 cm. If the sphere is completely submerged into water, by how much will the level of water rise in the cylindrical vessel ?

Ans :

Let the rise in level of water be h cm.

Radius of sphere = 3 cm. radius of cylinder

$$=\frac{12}{2}=6$$
 cm

Volume of water displaced in cylinder will be equal to the volume of sphere.

Thus

$$\pi \times 6 \times 6 \times h = \frac{4}{3} \times \pi \times 3 \times 3 \times 3$$
$$h = \frac{4 \times 3 \times 3 \times 3}{3 \times 6 \times 6} = 1 \text{ cm}$$

 $\pi r^2 h = \frac{4}{3}\pi r^3$

- 34. Hari, standing on the top of a building, sees the top of a tower at an angle of elevation of 50° and the foot of the tower at an angle of depression of 20°. Hari is 1.6 metre tall and the height of the building on which he is standing is 9.2 mitres. [3]
 - (a) Draw a rough sketch according to the given information.
 - (b) How far is the tower from the building?
 - (c) Calculate the height of the tower. $[\sin 20^\circ = 0.34, \cos 20^\circ = 0.94, \tan 20^\circ = 0.36]$

$$\sin 50^\circ = 0.77, \ \cos 50^\circ = 0.64, \ \tan 50^\circ = 1.19$$
]

Ans :

(a) Rough sketch



Hari is standing at D. His height BD is 1.6 m.

Height of the building, DF = 9.2 mThe angle of elevation of the top of the tower AG is 50°. The angle of depression of the foot of the tower is 20°. (b) Distance between the tower and the building,

$$BC = DE = FG$$

In right ΔBCG ,
 $\tan 20^{\circ} = \frac{CG}{BC} \Rightarrow 0.36 = \frac{1.6 + 9.2}{BC}$
$$BC = \frac{10.8}{0.36} = 30 \text{ m}$$

Hence, distance between the tower and the building = 30 m

(c) In right
$$\Delta ACB$$

 $AC = BC \tan 50^{\circ} = 30 \times 1.19$
 $= 35.7 \text{ m}$
Hence, height of the tower
 $= AC + CE + EG$

= 35.7 + 1.6 + 9.2 = 46.5 m

Section D

35. Show that 3 is a zero of the polynomial 2x² - x² - 13x - 6. Hence find all the zeroes of this polynomial. [4]
Ans :

$$\begin{array}{r} x-3 \overbrace{)2x^{2}+5x+2} \\ x-3 \overbrace{)2x^{3}-x^{2}-13x-6} \\ \underline{2x^{3}-6x^{2}} \\ 5x^{2}-13x-6 \\ \underline{5x^{2}-15x} \\ 2x-6 \\ \underline{2x-6} \\ 0 \\ p(x) = 2x^{2}-x^{2}-13x-6 \\ = 2(3)^{3}-(3)^{2}-13(3)-6 \\ = 2(27)-9-39-6 \\ = 54-54 = 0 \end{array}$$

So, x-3 is a factor of p(x).

by long division

Factorising the quotient, we get

$$= 3x^{2} + 4x + x + 2$$

= (2x + 1)(x + 2)
$$x = -\frac{1}{2}, -2$$

Hence, All the zeroes of p(x) are $-\frac{1}{2}, -2, 3$

or

Given that $x - \sqrt{5}$ is a factor of the polynomial $x^3 - 3\sqrt{5} x^2 - 5x + 15\sqrt{5}$, find all the zeroes of the polynomial.

Ans :

$$\begin{array}{r} x-\sqrt{5} \frac{x^2-2\sqrt{5} \ x-15}{x^3-3\sqrt{5} \ x^2-5x+15\sqrt{5}} \\ \frac{x^3-\sqrt{5} \ x^2}{-2\sqrt{5} \ x^2-5x+15\sqrt{5}} \\ \frac{-2\sqrt{5} \ x^2+10x}{-15x+15\sqrt{5}} \\ \frac{-15x+15\sqrt{5}}{0} \end{array}$$

Factorising the quotient we get

$$\begin{aligned} x^2 - 2\sqrt{5} x - 15 &= x^2 - 3\sqrt{5} x + \sqrt{5} x - 15 \\ &= x(x - 3\sqrt{5}) + \sqrt{5}(x - 3\sqrt{5}) \\ &= (x + \sqrt{5})(x - 3\sqrt{5}) \end{aligned}$$

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(1)

$$(x+\sqrt{5})(x-3\sqrt{5}) = 0 \Rightarrow x = \sqrt{5}, 3\sqrt{5}$$

All the zeroes are $\sqrt{5}, -\sqrt{5}$ and $3\sqrt{5}$.

36. A train covered a certain distance at a uniform speed. If the train would have been 10 km/hr scheduled time. And, if the train were slower by 10 km/hr, it would have taken 3 hr more than the scheduled time. Find the distance covered by the train. [4]

Ans :

Let the actual speed of the train be x km/hr and actual time taken y hr.

$$Distance = Speed \times Time$$

According to the given condition, we have

$$xy = (x+10)(y-2)$$

$$xy = xy - 2x + 10y - 20$$

$$2x - 10y + 20 = 0$$

$$x - 5y = -10$$

and

xy = (x - 10)(y + 3)xy = xy + 3x - 10y - 30

3x

$$-10u = 30$$
 ...(2)

Multiplying equation (1) by 3 and subtracting equation (2) from equation (1),

$$3 \times (x - 5y) - (3x - 10y) = -3 \times 10 - 30$$

 $-5y = -60$
 $y = 12$

Substituting value of y equation (1),

 $x - 5 \times 12 = -10$

or,
$$x = -10 + 60$$

or, x = 50

Hence, the distance covered by the train

$$= 50 \times 12$$

= 600 km.

37. In the figure, $\angle BED = \angle BDE$ and E is the midpoint of BC. Prove that $\frac{AF}{CF} = \frac{AD}{BE}$. [4]



Ans :

We have redrawn the given figure as below. Here $CG \mid\mid FD$.



We have $\angle BED = \angle BDE$ Since *E* is mid-point of *BC*,

or,
$$BE = BD = EC$$
 ...(1)
In ΔBCG , $DE \parallel FG$

 $\frac{BD}{DG} = \frac{BE}{EC} = 1 \qquad (\text{from (1)})$

$$BD = DG = EC = BE$$
 [using (1)]

$$CG || FD$$

$$\frac{AG}{GD} = \frac{AC}{CF}$$
(By BPT)

$$\frac{AG + GD}{GD} = \frac{AF + CF}{CF}$$
,
$$\frac{AD}{GD} = \frac{AF}{CF}$$
Thus
$$\frac{AF}{CF} = \frac{AD}{BE}$$
 (using (1))
or

In the given figure, D and E trisect BC. Prove that $8AE^2 = 3AC^2 + 5AD^2$.

Ans :

In ΔADF ,

As per given condition we have drawn the figure below.

Since D and E trisect BC, let BD = DE = EC be x. Then BE = 2x and BC = 3xIn $\triangle ABE$, $AE^2 = AB^2 + BE^2 = AB^2 + 4x^2$...(1)

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In
$$\triangle ABC$$
, $AC^{e} = AB^{2} + BC^{e} = AB^{2} + 9x^{2}$...(2)
In $\triangle ADB$, $AD^{2} = AB^{2} + BD^{2} = AB^{2} + x^{2}$...(3)
Multiplying (2) by 3 and (3) by 5 and adding we have

$$3AC^{2} + 5AD^{2} = 3(AB^{2} + 9x^{2}) + (AB^{2} + x^{2})$$

= $3AB^{2} + 27x^{2} + 5AB^{2} + 5x^{2}$
= $8AB^{2} + 32x^{2}$
= $8(AB^{2} + 4x^{2}) = 8AE^{2}$

Thus $3AC^2 + 5AD^2 = 8AE^2$ Hence Proved

38. Evaluate : [4] $\sin^2 30^\circ \cos^2 45^\circ + 4 \tan^2 30^\circ + \frac{1}{2} \sin 90^\circ - 2 \cos^2 90^\circ + \frac{1}{24}$

Ans :

 $\sin^2 30^{\circ} \cos^2 45^{\circ} + 4 \tan^2 30^{\circ} + \frac{1}{2} \sin 90^{\circ} - 2 \cos^2 90^{\circ} + \frac{1}{24}$

$$= \left(\frac{1}{2}\right)^2 \times \left(\frac{1}{\sqrt{2}}\right)^2 + 4\left(\frac{1}{\sqrt{3}}\right)^2 + \frac{1}{2}(1)^2 - 2(0) + \frac{1}{24}$$
$$= \frac{1}{4}\left(\frac{1}{2}\right) + \frac{4}{3} + \frac{1}{2} + \frac{1}{24} = \frac{1}{8} + \frac{4}{3} + \frac{1}{2} + \frac{1}{24}$$
$$= \frac{3 + 32 + 12 + 1}{24} = \frac{48}{24} = 2$$

Prove that : $\frac{\tan\theta}{1-\cot\theta} + \frac{\cot\theta}{1-\tan\theta} = 1 + \tan\theta + \cot\theta$. Ans :

$$\frac{\tan\theta}{1-\cot\theta} + \frac{\cot\theta}{1-\tan\theta} = \frac{\tan\theta}{1-\frac{1}{\tan\theta}} + \frac{\frac{1}{\tan\theta}}{1-\tan\theta}$$
$$= \frac{\tan^2\theta}{\tan\theta-1} + \frac{1}{(1-\tan\theta)\tan\theta}$$
$$= \frac{\tan^2\theta}{\tan\theta-1} - \frac{1}{(\tan\theta-1)\tan\theta}$$
$$= \frac{\tan^3\theta-1}{(\tan\theta-1)\tan\theta}$$
$$[\because a^3 - b^3 = (a-b)(a^2 + b^2 + ab)]$$
$$= \frac{(\tan\theta-1)(\tan^2\theta + \tan\theta + 1)}{(\tan\theta-1)(\tan\theta)}$$
$$= \frac{\tan^2\theta + \tan\theta + 1}{\tan\theta}$$
$$= \tan\theta + 1 + \cot\theta$$

Hence Proved.

39. If A(-4,8), B(-3,-4), C(0,-5) and D(5,6) are the vertices of a quadrilateral ABCD, find its area. [4] Ans:

We have
$$A(-4,8)$$
, $B(-3, -4)$, $C(0,5)$ and $D(5,6)$
Area of quadrilateral

$$= \frac{1}{2}[(x_1y_2 - x_2y_1) + (x_2y_3 - x_3y_2) + (x_3y_4 - x_4y_3) + (x_4y_1 - x_1y_4)]$$
Area $= \frac{1}{2}[\{-4 \times (-4) - (-3)(8)\} + \{(-3)(-5) - 0 \times (-4)\} + \{0 \times 6 - 5(-5)\} + [\{5 \times 8 - (-4)(6)\}]$

$$= \frac{1}{2}[16 + 24 + 15 - 0 + 0 + 25 + 40 + 24]$$

$$= \frac{1}{2}[40 + 15 + 25 + 40 + 24]$$

$$=\frac{1}{2} \times 144 = 72$$
 sq. units

40. An elastic belt is placed around the rim of a pulley of radius 5 cm. From one point C on the belt elastic belt is pulled directly away from the centre O of the pulley until it is at P, 10 cm from the point O. Find the length of the belt that is still in contact with the pulley. Also find the shaded area.

Ans :

Here AP is tangent at point A on circle.

Thus
$$\angle OAP = 90^{\circ}$$

Now $\cos \theta = \frac{OA}{OP} = \frac{5}{10} = \frac{1}{2}$
or, $\theta = 60^{\circ}$
Reflex $\angle AOB = 360^{\circ} - 60^{\circ} - 60^{\circ} = 240^{\circ}$
Now $\operatorname{arc} ADB = \frac{2 \times 3.14 \times 5 \times 120}{360}$
 $= 20.93 \operatorname{cm}$
Hence length of elastic in contact = 20.93 cm
Now, $AP = 5\sqrt{3} \operatorname{cm}$
Area, $(\Delta OAP + \Delta OBP) = 25\sqrt{3} = 43.25 \operatorname{cm}^2$
Area of sector, $OACB = \frac{25 \times 3.14 \times 120}{360}$
 $= 26.16 \operatorname{cm}^2$.
Shaded Area = $43.25 - 26.16$
 $= 17.09 \operatorname{cm}^2$

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